

# Neutrino-Induced Coherent Pion Production

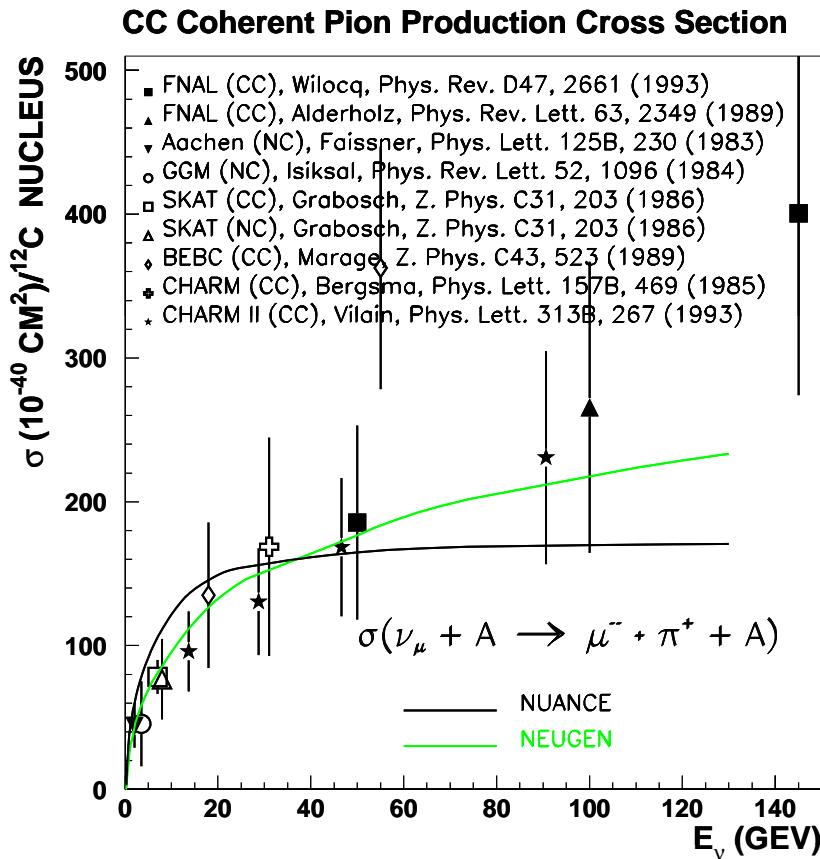
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# Introduction

- $\nu$ -induced coherent  $\pi$  production reactions:
  - Charged Current  $\nu_l A \rightarrow l^- \pi^+ A$
  - Neutral Current  $\nu_l A \rightarrow \nu_l \pi^0 A$
- Important for oscillation experiments: systematic uncertainties
  - Example:  $\nu_l A \rightarrow \nu_l \pi^0 X \leftarrow$  background for  $\nu_e$  appearance
- Also interesting for hadronic and nuclear physics:
  - N, N-R axial form factors
  - Nuclear correlations
  - $\pi$  in the nuclear medium
- Measured at high energies  $E_\nu > 2$  GeV (FNAL, GGM, SKAT, BEBC, ...)

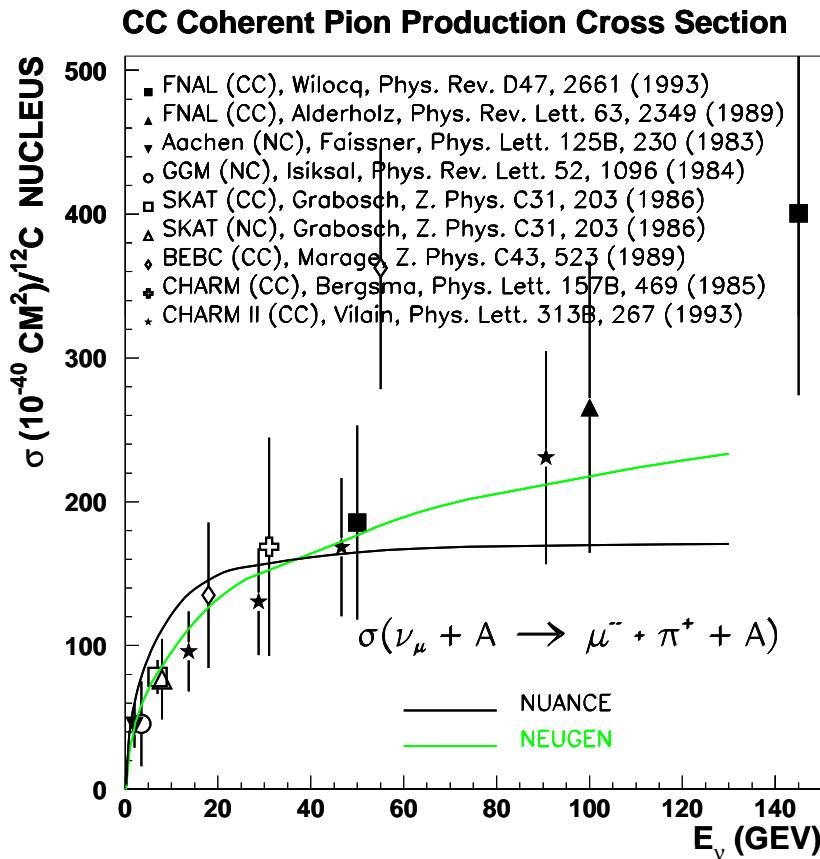
# Introduction



- G. Zeller, hep-ex/0312061 (NUINT 02)
- Data scaled to  $^{12}\text{C}$  assuming  $A^{1/3}$  dependence
- $\sigma(\text{CC})=2 \sigma(\text{NC})$

- Measured at high energies  $E_\nu > 2$  GeV (FNAL, GGM, SKAT, BEBC, ...)

# Introduction



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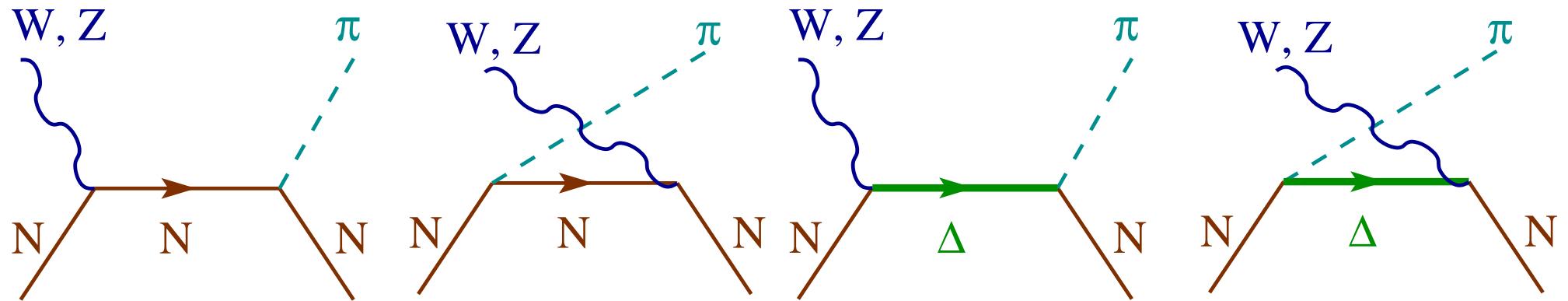
- Measured at high energies  $E_\nu > 2 \text{ GeV}$  (FNAL, GGM, SKAT, BEBC, ...)
- These data are well described by models based on PCAC  
Rein & Sehgal, NPB 223 (83), Paschos, Kartavtsev, Gounaris, PRD 74(06)  
However, at lower energies ...

# Introduction

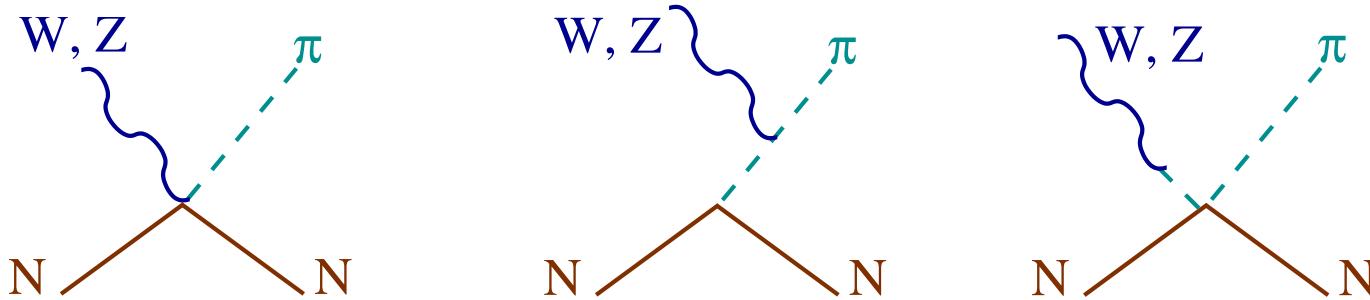
- K2K ( $< E_\nu > = 1.3 \text{ GeV}$ ) finds a **significant deficit** of  $\mu^-$  at forward angles
- Upper bound for **CC** Coh.  $\pi^+$  production below theoretical expectations
- MiniBooNE ( $< E_\nu > = 0.75 \text{ GeV}$ ) **NC**  $\pi^0$  data under analysis.
  - First results: J. Link @ NUINT07, arXiv:0709.3213
- Our goal: theoretical study of **CC** and **NC** Coherent  $\pi$  production at intermediate energies ( $E_\nu \sim 1 \text{ GeV}$ ) improving the calculations of : Kelkar et al, PRC 55 (97), Singh et al, PRL 96 (06)
  - Complete relativistic elementary amplitude
  - Hadronic degrees of freedom:  $\pi$ ,  $N$ ,  $\Delta(1232)$
  - Renormalization of the  $\Delta$  properties in the nuclear medium
  - Realistic treatment of  $\pi$  distortion

# The model

- Elementary mechanisms: Hernandez, Nieves & Valverde, PRD 76 (07)



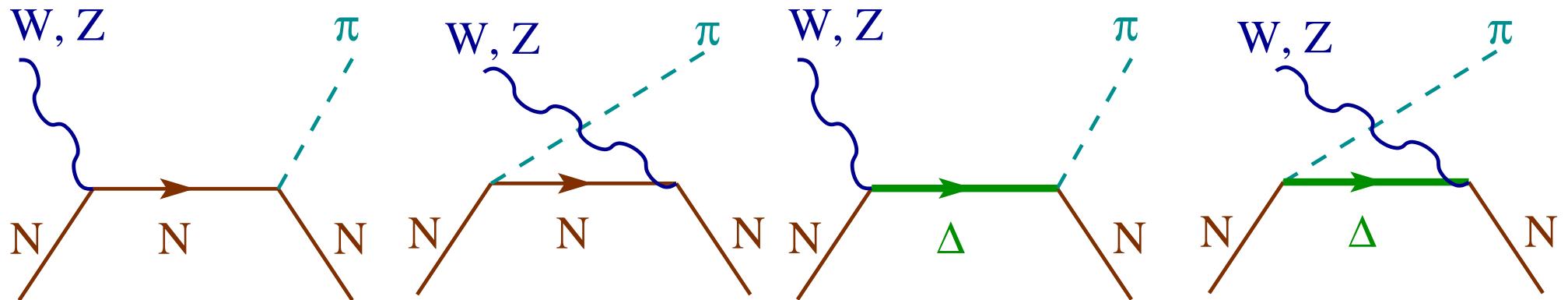
- Other contributions



cancel for **isospin symmetric** nuclei

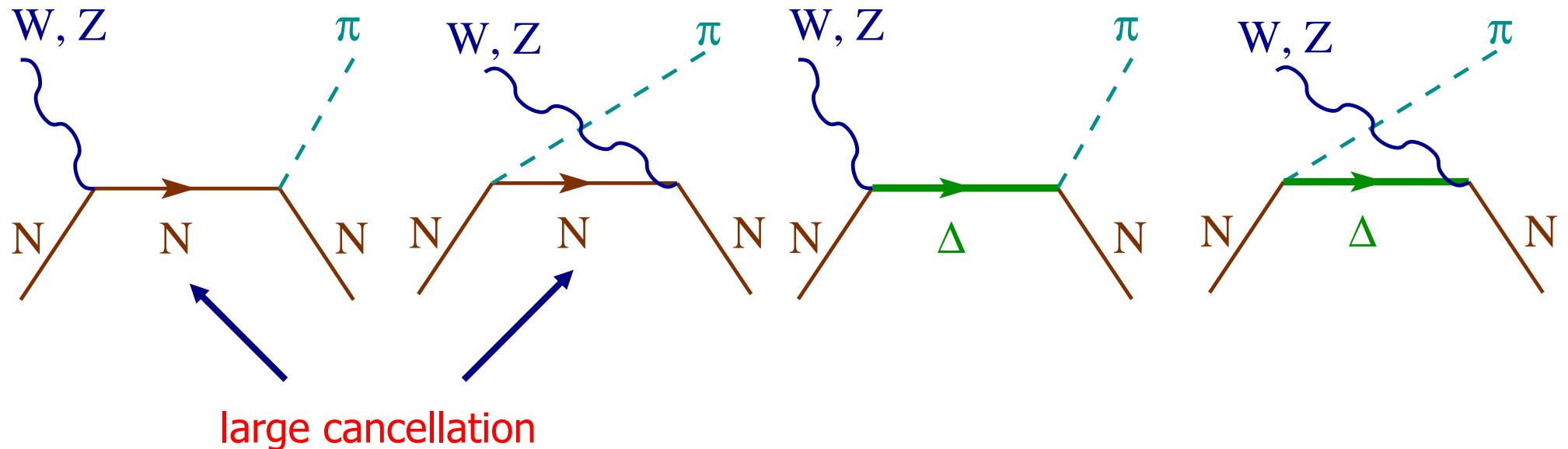
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- Elementary mechanisms: Hernandez, Nieves & Valverde, PRD 76 (07)



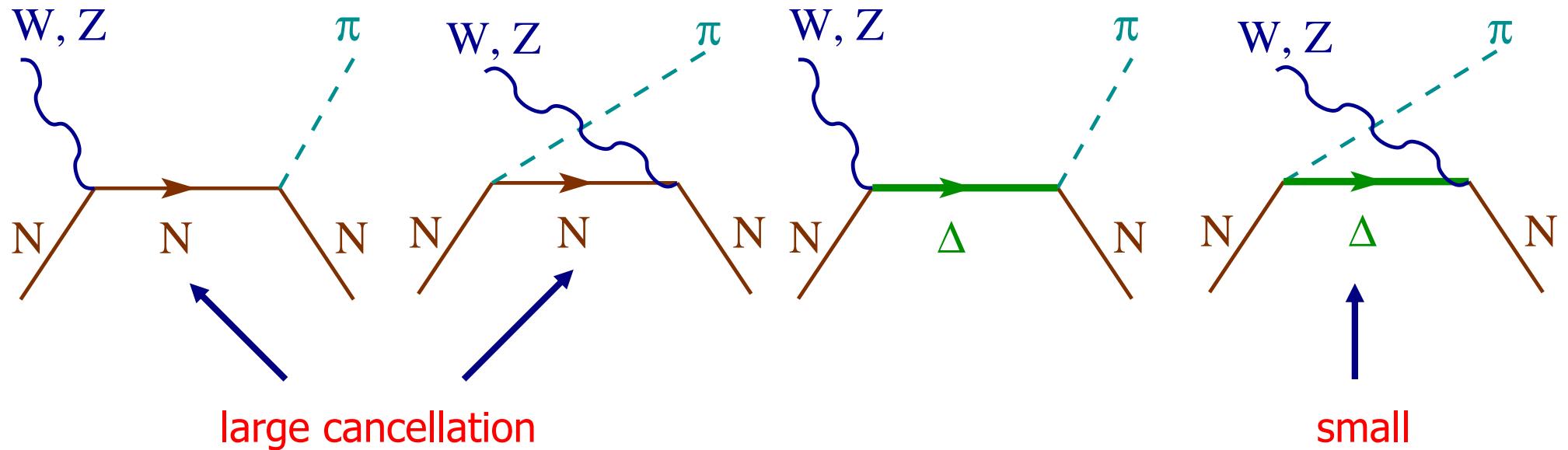
# The model

- Elementary mechanisms: Hernandez, Nieves & Valverde, PRD 76 (07)



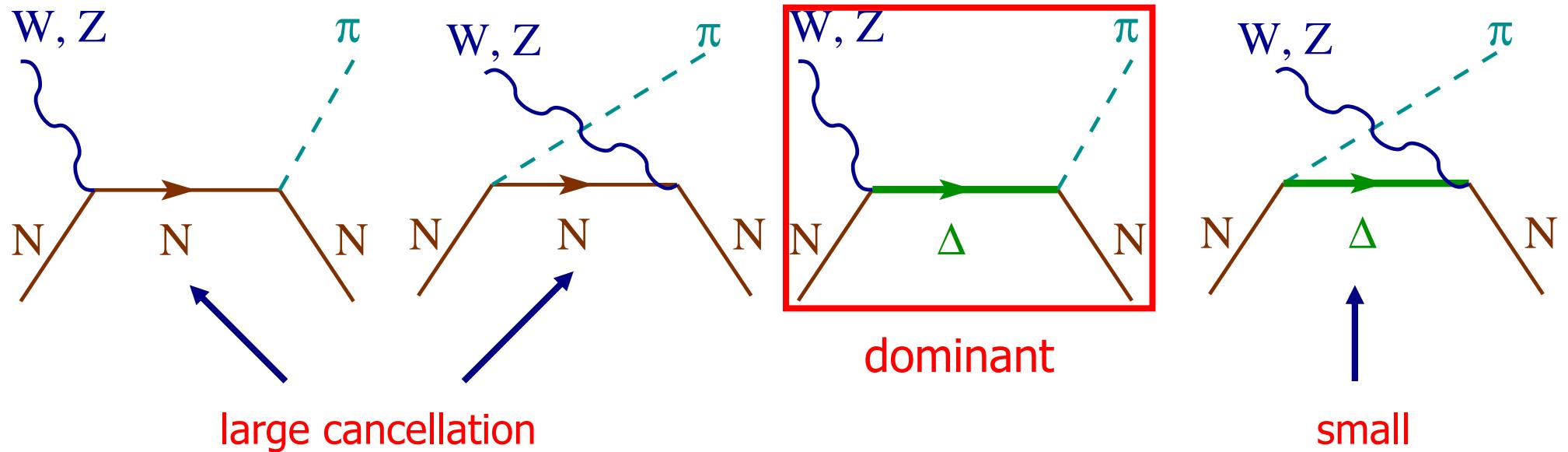
# The model

- Elementary mechanisms: Hernandez, Nieves & Valverde, PRD 76 (07)



# The model

- Elementary mechanisms: Hernandez, Nieves & Valverde, PRD 76 (07)



# Formalism

- The amplitude for CC  $\pi^+$  production:  $\mathcal{M}_c = \frac{G}{\sqrt{2}} \cos \theta_c \not{l}_\mu J^\mu$
- $J^\mu \leftarrow$  Nuclear current  $\leftrightarrow$  sum over all nucleons
- For the dominant direct  $\Delta$  mechanism:

$$J^\mu_{IA} = -\frac{\sqrt{3}}{2} i \int d\vec{r} e^{i(\vec{q}-\vec{p}_\pi) \cdot \vec{r}} \left[ \rho_p(r) + \frac{\rho_n(r)}{3} \right] \frac{f^*}{m_\pi} D_\Delta p_\pi^\alpha \text{Tr} \left\{ \bar{u} \Lambda_{\alpha\beta} \mathcal{A}^{\beta\mu} u \right\}$$

$D_\Delta \leftarrow$  propagator       $\Lambda_{\alpha\beta} \leftarrow$  spin 3/2 projection operator

$$\begin{aligned} \mathcal{A}^{\beta\mu} = & \left( \frac{C_3^V}{M} (g^{\beta\mu} q^\mu - q^\beta \gamma^\mu) + \frac{C_4^V}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + \frac{C_5^V}{M^2} (g^{\beta\mu} q \cdot p - q^\beta p^\mu) + g^{\beta\mu} C_6^V \right) \gamma_5 \\ & + \frac{C_3^A}{M} (g^{\beta\mu} q^\mu - q^\beta \gamma^\mu) + \frac{C_4^A}{M^2} (g^{\beta\mu} q \cdot p' - q^\beta p'^\mu) + C_5^A g^{\beta\mu} + \frac{C_6^A}{M^2} q^\beta q^\mu \end{aligned}$$

- Form factors:  $C_{3,4,5}^V \leftarrow$  e N scattering     $C_6^V = 0 \leftarrow$  CVC

$$C_6^A = C_5^A \frac{M^2}{m_\pi^2 - q^2} \leftarrow \text{PCAC}$$

$$C_4^A = -\frac{1}{4} C_5^A \quad C_3^A = 0 \leftarrow \text{Adler model}$$

# Formalism

- There are different parametrizations of  $C_5^A$  in the literature:

- set I  $C_5^A = C_5^A(0) \left(1 + \frac{1.21 q^2}{2 \text{ GeV}^2 - q^2}\right) \left(1 - \frac{q^2}{M_{A\Delta}^2}\right)^{-2}$

$$C_5^A(0) = \frac{g_{\Delta N\pi} f_\pi}{\sqrt{6} M} \approx 1.2 \leftarrow \text{off-diagonal GT relation}$$

$M_{A\Delta} = 1.28 \text{ GeV} \leftarrow$  extracted from BNL data  
Kitagaki et al. PRD42 (90)

- set II  $C_5^A = C_5^A(0) \left(1 - \frac{q^2}{3M_{A\Delta}^2}\right)^{-1} \left(1 - \frac{q^2}{M_{A\Delta}^2}\right)^{-2}$

$C_5^A(0) = 0.867 \pm 0.075 \leftarrow$  extracted from ANL data  
with  $W_{N\pi} < 1.4 \text{ GeV}$   
 $M_{A\Delta} = 0.985 \pm 0.082 \text{ GeV} \leftarrow$  Hernandez,Nieves,Valverde PRD 76 (07)

- Coherent  $\pi$  production is very sensitive on  $C_5^A(0)$

# Formalism

- For  $\nu_l p \rightarrow l^- \Delta$  at  $q^2=0$  ( $m_\ell = 0$ )

$$\frac{d\sigma}{dq^2}(q^2 = 0) \propto [C_5^A(0)]^2$$

- Axial coupling  $C_5^A(0)$  values in the literature,  
adapted from Barquilla-Cano, Buchmann, Hernandez PRC 75 (07)

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Quark models	0.97, 0.83, 1.17, 1.06, 0.87, 1.5, 0.93
Empirical approaches	$1.15 \pm 0.23$ , $1.39 \pm 0.14$ , $1.1 \pm 0.2$ , $1.22 \pm 0.06$ , $0.867 \pm 0.075$
Current Algebra	0.98

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# Formalism

## ■ Delta in the medium:

$$D_{\Delta} \Rightarrow \tilde{D}_{\Delta}(r) = \frac{1}{(W + M_{\Delta})(W - M_{\Delta} - \text{Re}\Sigma_{\Delta}(\rho) + i\tilde{\Gamma}_{\Delta}/2 - i\text{Im}\Sigma_{\Delta}(\rho))}$$

$\tilde{\Gamma}_{\Delta} \leftarrow$  Free width  $\Delta \rightarrow N \pi$  modified by Pauli blocking

$$\text{Re}\Sigma_{\Delta}(\rho) \approx 40 \text{ MeV} \frac{\rho}{\rho_0}$$

$\text{Im}\Sigma_{\Delta}(\rho) \leftarrow$  many-body processes:

- $\Delta N \rightarrow N N$
- $\Delta N \rightarrow N N \pi$
- $\Delta N N \rightarrow N N N$

# Formalism

## Pion distortion:

$$e^{-i\vec{p}_\pi \cdot \vec{r}} \rightarrow \phi_{out}^*(\vec{p}_\pi, \vec{r}) \quad \vec{p}_\pi e^{-i\vec{p}_\pi \cdot \vec{r}} \rightarrow i\vec{\nabla} \phi_{out}^*(\vec{p}_\pi, \vec{r})$$

$\phi_{out}^*(\vec{p}_\pi, \vec{r}) \leftarrow$  solution of the Klein-Gordon equation

$$\left( -\vec{\nabla}^2 - \vec{p}_\pi^2 + 2\omega_\pi \hat{V}_{\text{opt}} \right) \phi_{out}^* = 0$$

$\hat{V}_{\text{opt}}(\vec{r}) \leftarrow$  optical potential in the  $\Delta$ -hole model:  
Nieves, Oset & Garcia Recio NPA 554 (93)

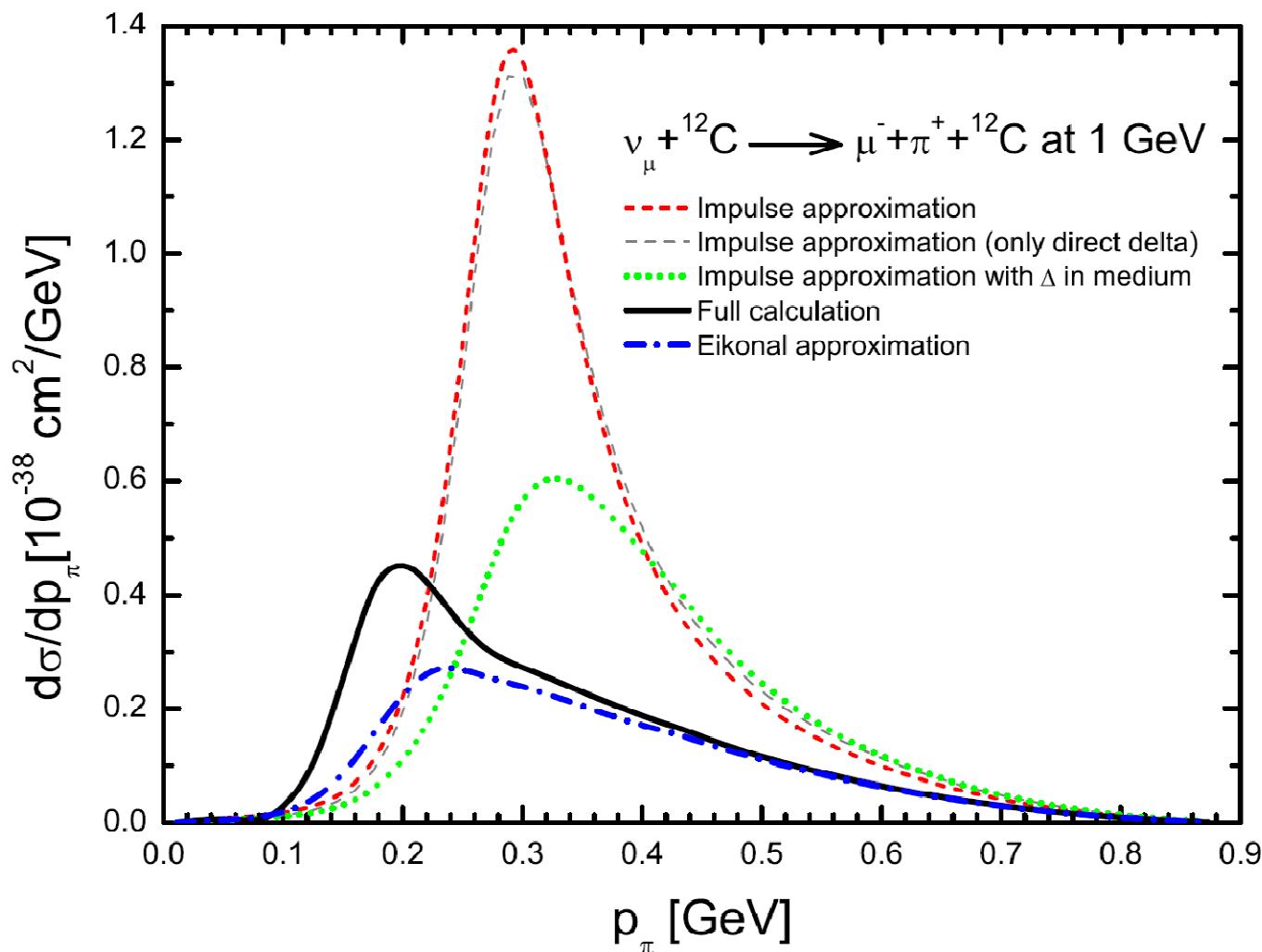
$$2\omega_\pi \hat{V}_{\text{opt}}(\vec{r}) = 4\pi \frac{M^2}{s} \left[ \vec{\nabla} \cdot \frac{\mathcal{P}(r)}{1 + 4\pi g' \mathcal{P}(r)} \vec{\nabla} - \frac{1}{2} \frac{\omega}{M} \Delta \frac{\mathcal{P}(r)}{1 + 4\pi g' \mathcal{P}(r)} \right]$$

$g'=0.63 \leftarrow$  Landau-Migdal parameter

$$\mathcal{P} = -\frac{1}{6\pi} \left( \frac{f^*}{m_\pi} \right)^2 \left\{ \frac{\rho_p + \rho_n/3}{\sqrt{s} - M_\Delta - \text{Re}\Sigma_\Delta + i\tilde{\Gamma}_\Delta/2 - i\text{Im}\Sigma_\Delta} + \frac{\rho_n + \rho_p/3}{-\sqrt{s} - M_\Delta + 2M - \text{Re}\Sigma_\Delta} \right\}$$

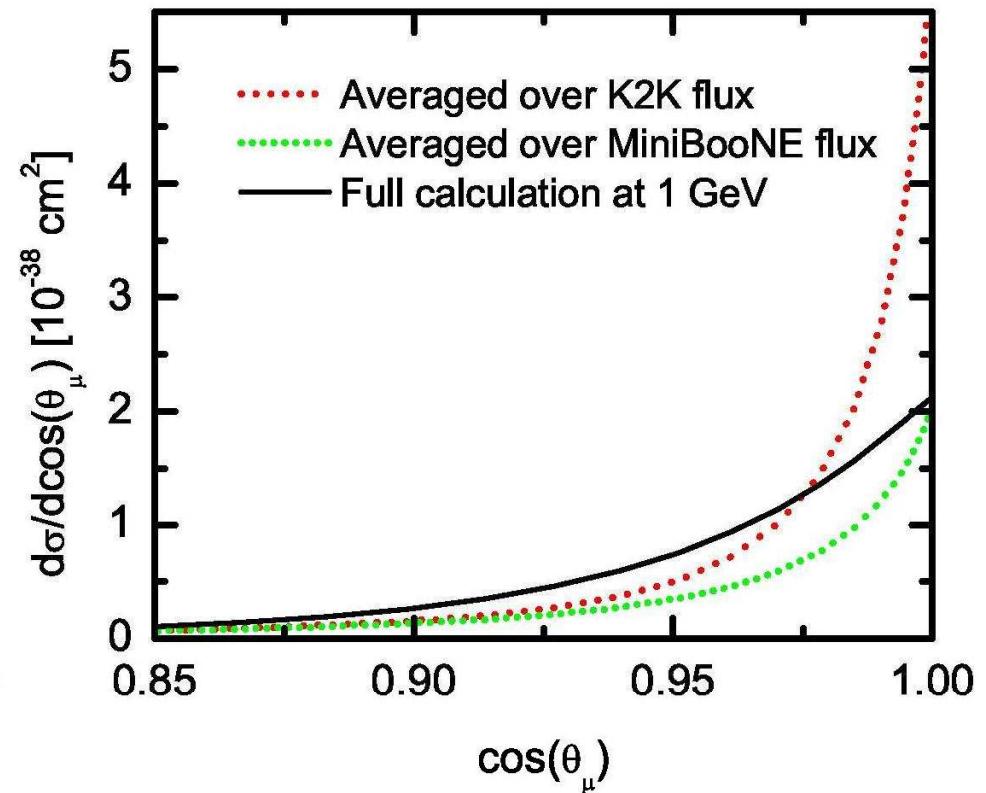
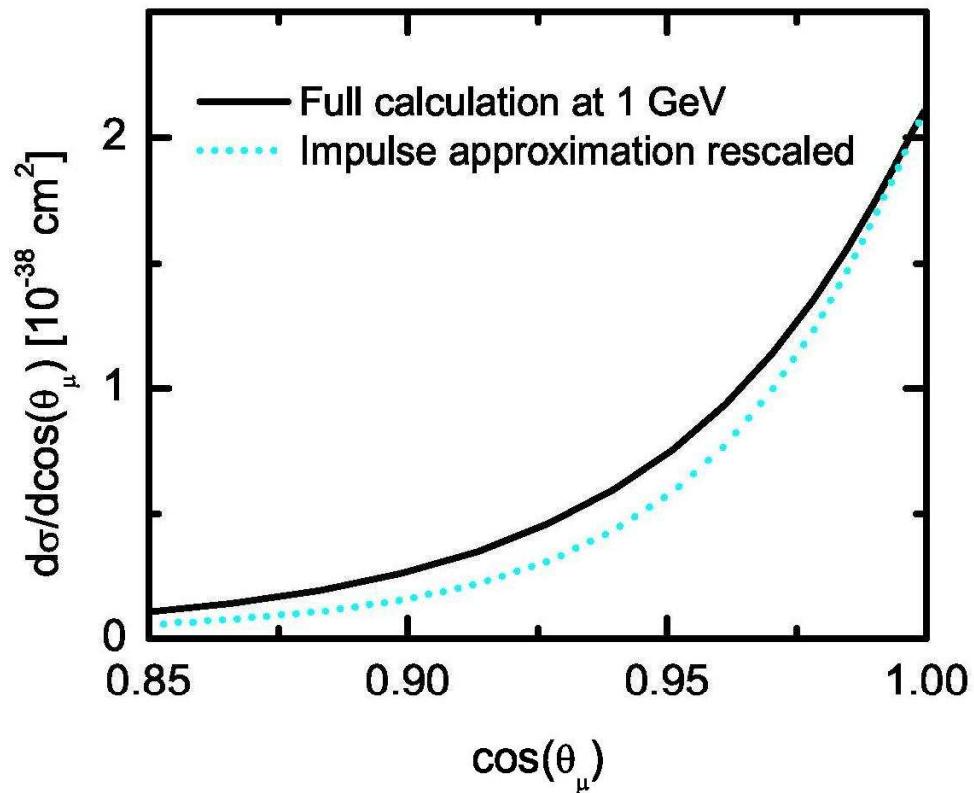
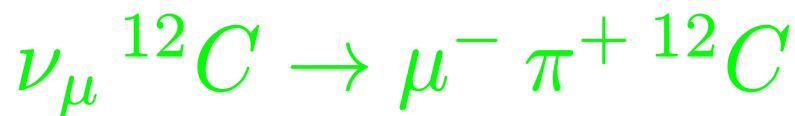
↑      ↑  
 Direct    Crossed  
 $\Delta$ -hole excitations

# Results



- Medium effects reduce considerably de cross section
- Pion distortion shifts down the peak
- Eikonal fails for  $p_\pi < 400$  MeV

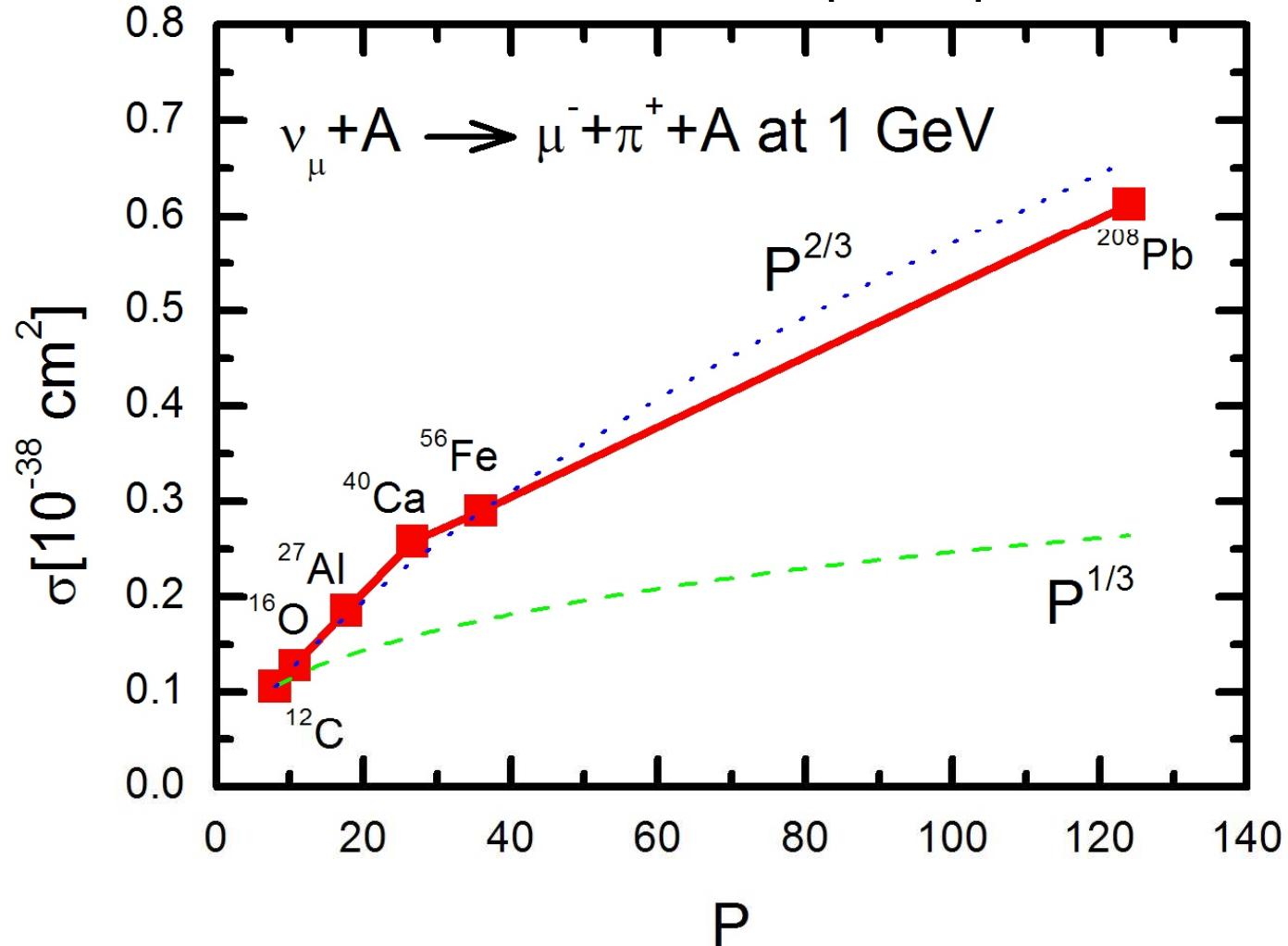
# Results



- Muon angular distribution relatively unaffected by the medium
- Presence of higher energy  $\nu \Rightarrow$  narrower angular distributions

# Results

- Dependence on the effective number of participants  $P=Z+N/3$  (for CC)

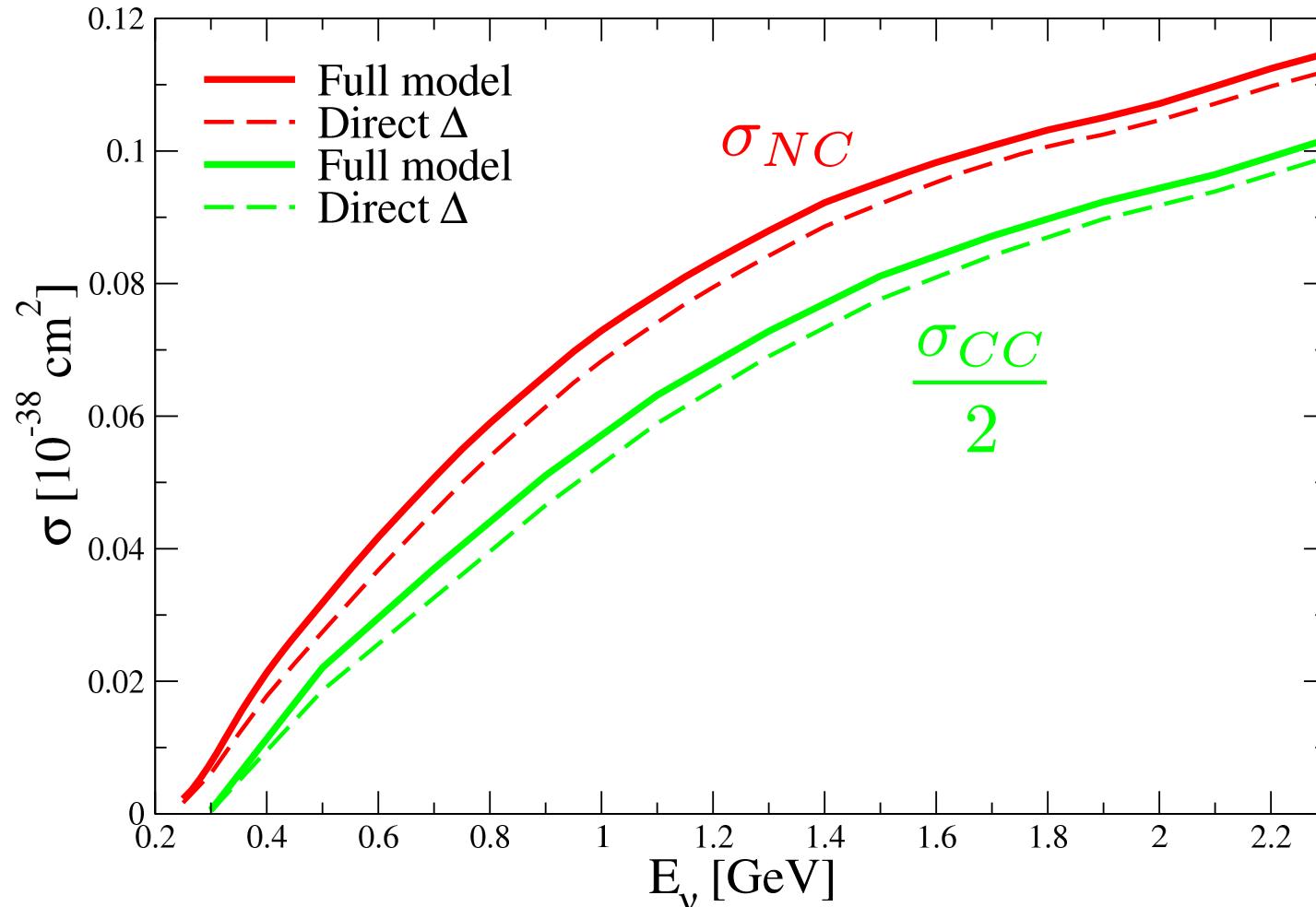


$\sigma \sim P^{2/3}$  ↔

- strong pion absorption forces de reaction to be **peripheral**
- effect of the nuclear form factor on heavier nuclei

# Results

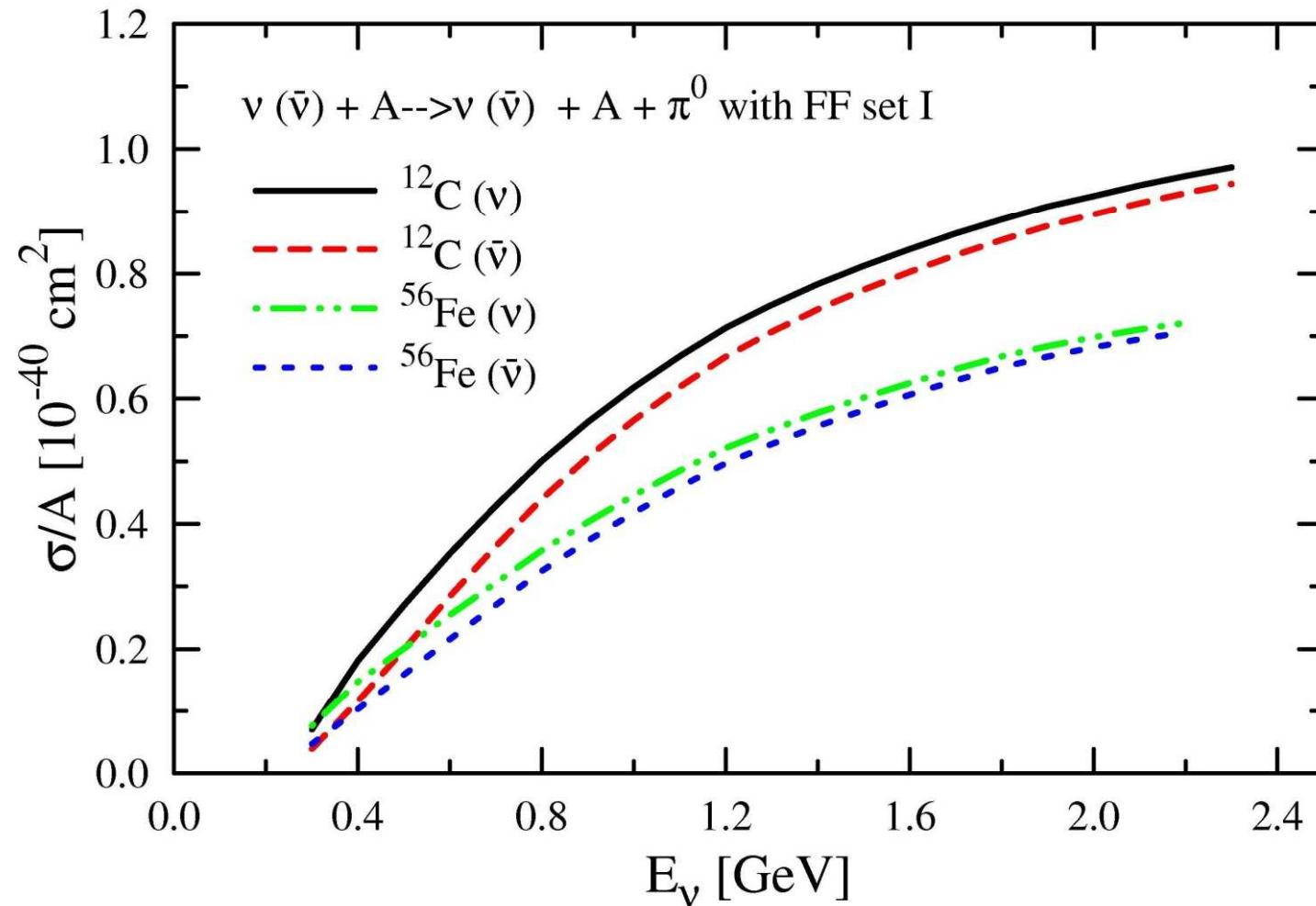
- NC Coherent Pion Production:  $\nu_\mu \ ^{12}C \rightarrow \nu_\mu \ \pi^0 \ ^{12}C$



$$\sigma_{NC} \neq \frac{\sigma_{CC}}{2} \leftrightarrow \begin{array}{l} \text{Phase Space: } m_\mu \neq 0 \\ \text{Interference terms: } q^2 \neq 0 \text{ contributions} \end{array}$$

# Results

## ■ NC Coherent Pion Production: $\nu$ vs. $\bar{\nu}$



- $\sigma(\nu) \neq \sigma(\bar{\nu}) \leftrightarrow q^2 \neq 0$  contributions (interference terms)
- The difference is slightly larger for lighter nuclei

# Results

- Predictions and Comparison to experiment: [units of  $10^{-40} \text{ cm}^2$ ]

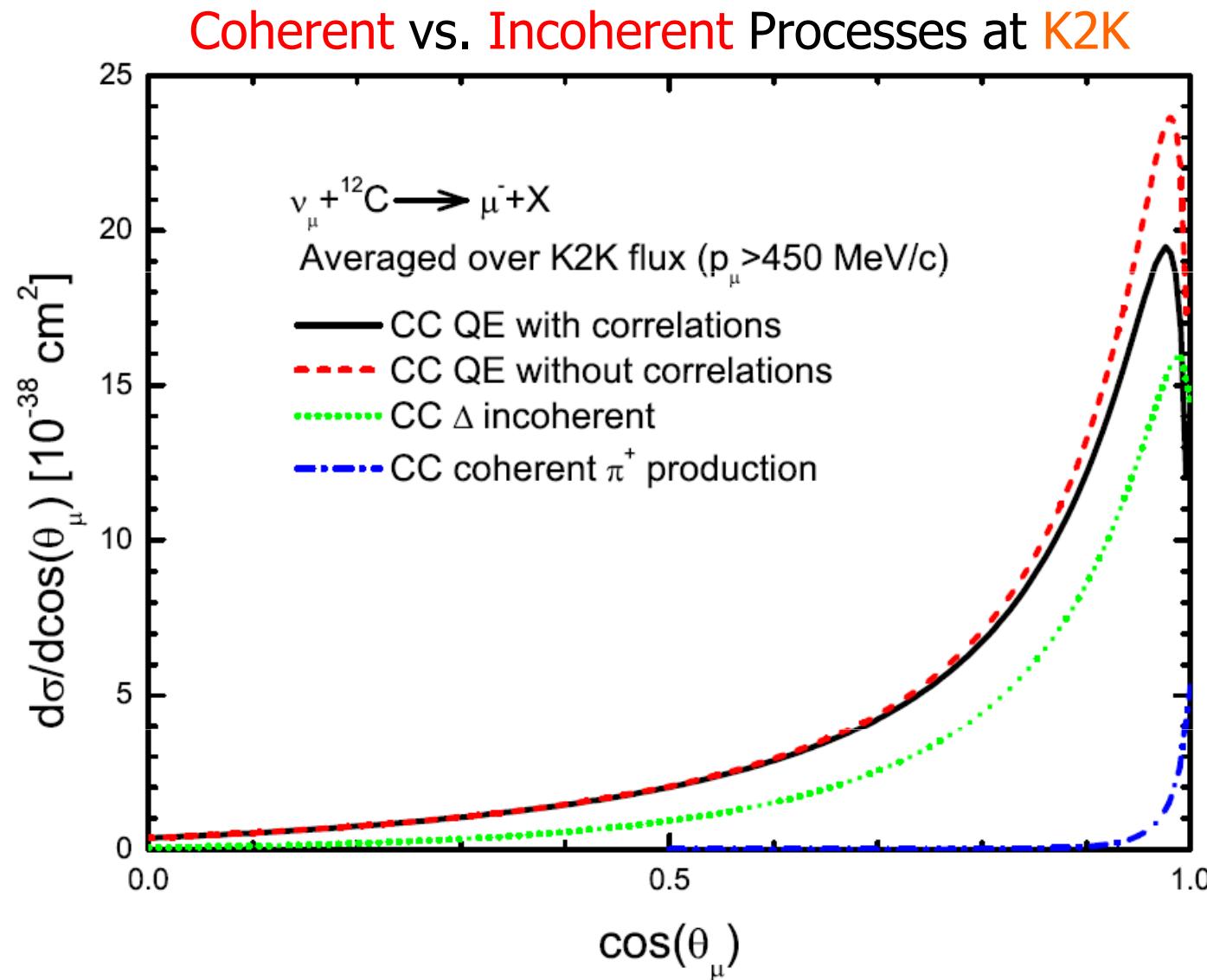
Reaction	Experiment	$\sigma_I$	$\sigma_{II}$	$\sigma$ Experimental
NC $\nu + {}^{27}\text{Al}$	Aachen-Padova	19.9	10.1	$29 \pm 10$
NC $\bar{\nu} + {}^{27}\text{Al}$	Aachen-Padova	19.7	9.8	$25 \pm 7$
CC $\nu + {}^{12}\text{C}$	K2K	10.8	5.7	$< 7.7$
NC $\nu + {}^{12}\text{C}$	MiniBooNE	5.0	2.6	-
NC $\bar{\nu} + {}^{12}\text{C}$	MiniBooNE	4.6	2.2	-

- Differences between sets I & II  $\longleftrightarrow \sigma(\text{I})/\sigma(\text{II}) \sim \left[ C_{5(\text{I})}^A(0)/C_{5(\text{II})}^A(0) \right]^2 \approx 1.9$

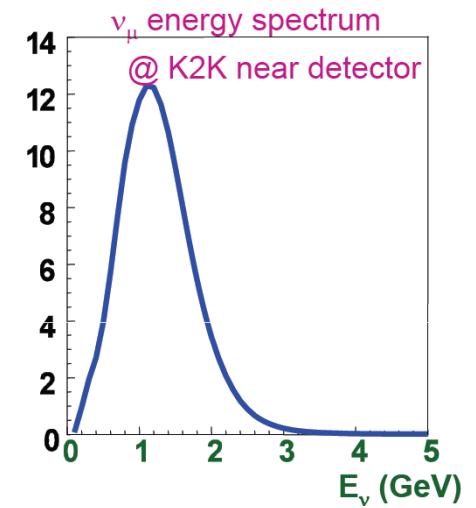
- Reasons for the discrepancies:

- Axial N- $\Delta$  not sufficiently constrained (more data needed)
- More complete theoretical description of the elementary amplitude (heavier resonances) required
- Optical potential at lower and higher energies can be improved
- Difficulties in the experimental separation of coherent and incoherent processes:

# Results

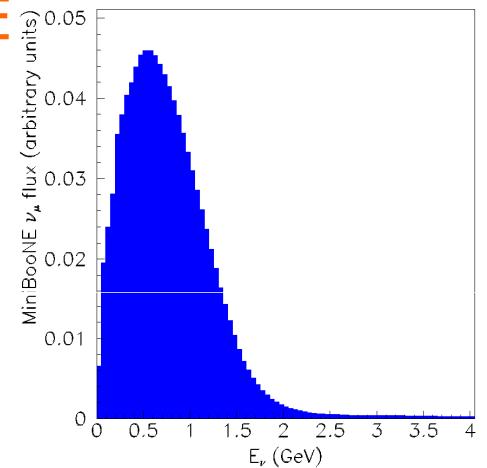
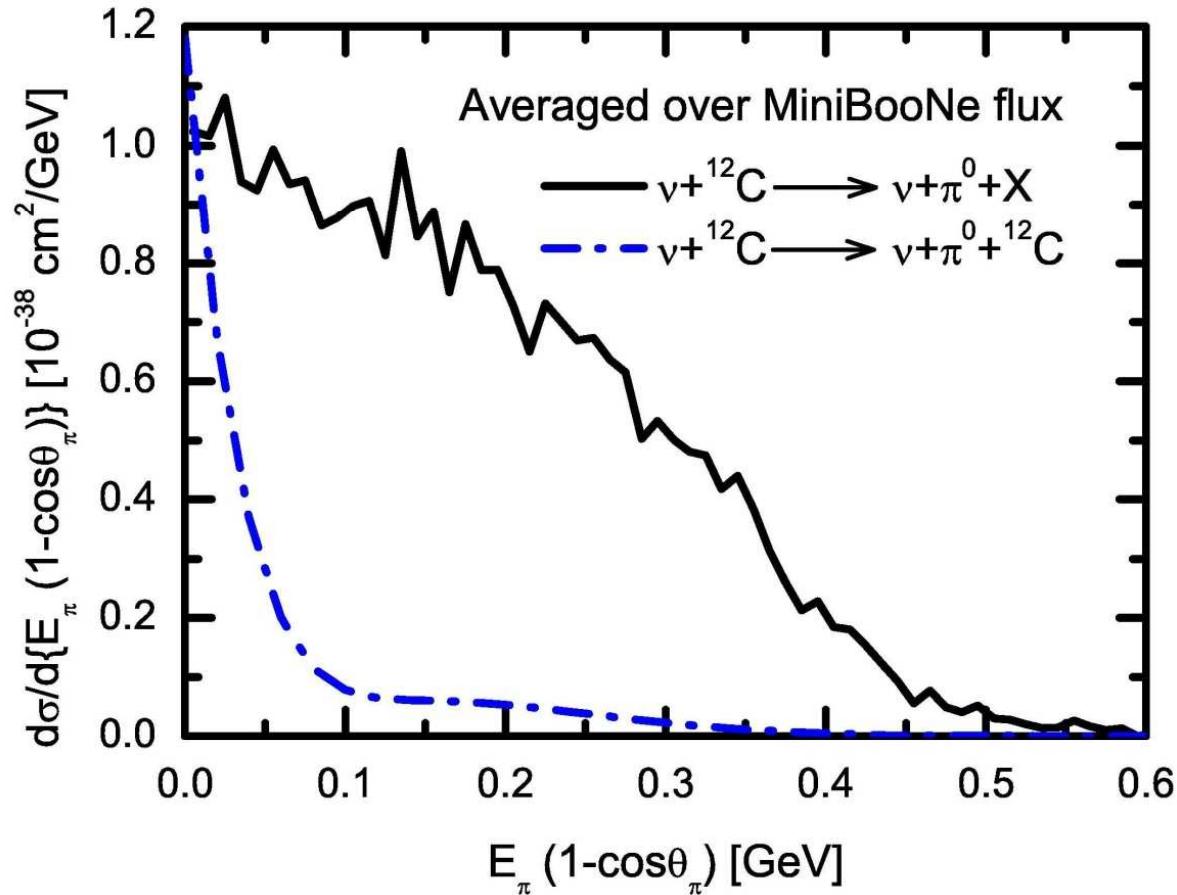


The coherent cross section might be considerably **smaller** than the **Impulse Approximation** prediction but still **bigger** than the **K2K upper limit**



# Results

## ■ Coherent & Incoherent NC $\pi^0$ Production @ MiniBooNE



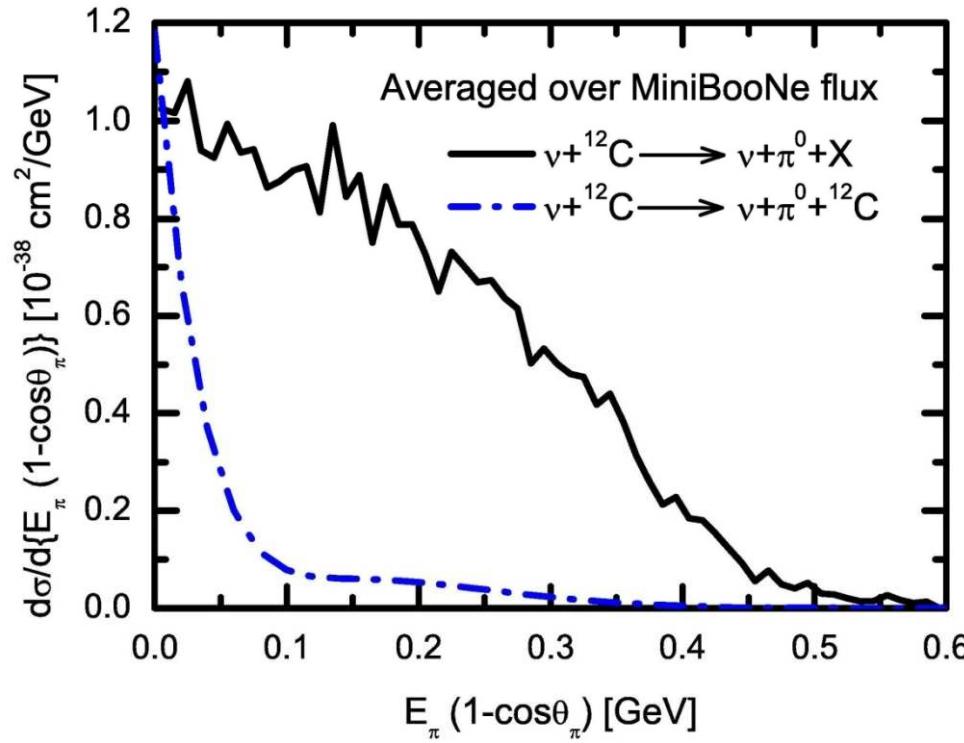
Coherent fraction

$$\frac{\sigma(\text{coh.})}{\sigma(\text{coh.}) + \sigma(\text{incoh.})} = 0.14$$

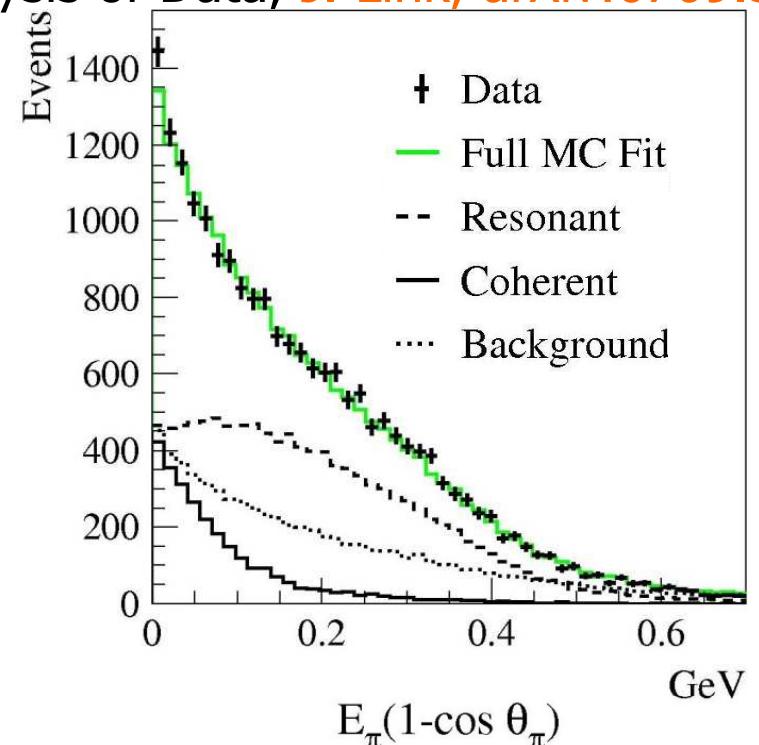
- Incoherent reaction studied with the GiBUU transport model  
T. Leitner, L. Alvarez-Ruso & U. Mosel, PRC 74 (06)

# Results

## ■ Coherent & Incoherent NC $\pi^0$ Production @ MiniBooNE



Analysis of Data, J. Link, arXiv:0709.3213



Coherent fraction  $\frac{\sigma(\text{coh.})}{\sigma(\text{coh.}) + \sigma(\text{incoh.})} = 0.14$

$19 \pm 1.1(\text{stat}) \pm 2.5 (\text{sys}) \%$

## ■ Exp. Analysis based on the R&S model:

- Raw MC predicts a coherent fraction of 30 %
- The coherent axial mass has to be reduced by 3 to get agreement with data

# Conclusions

- Theoretical study of CC & NC coherent pion production:
  - Complete relativistic elementary amplitude in terms of  $\pi$ , N,  $\Delta(1232)$
  - Nuclear form factor in the Impulse Approximation
  - Renormalization of the  $\Delta$  properties in the nuclear medium
  - $\pi$  distortion  $\leftrightarrow$  KG equation with a realistic optical potential
- Nuclear effects significantly reduce the coherent cross section
- Results depend strongly on  $C_5^A(0)$
- $\sigma \sim P^{2/3}$  with  $P=(Z+N/3)$  for CC and  $P=A$  for NC
- We predict a 14 % coherent fraction @ MiniBooNE (on  $^{12}\text{C}$ )
- The experimental separation between coherent and incoherent processes is model dependent and should be handled with care